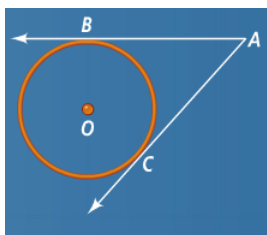


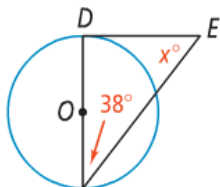
Lesson 12.1 Tangent lines

A tangent to a circle is a line in the plane of the circle that intersects the circle in exactly one point.

That point is called the point of tangency. Ray AB is tangent to circle O at B . Ray AC is tangent at point C .



1 Segment ED is tangent to circle O at D . What is the value of x ?

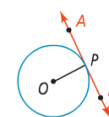


Ex. What is the distance to the horizon that a person can see on a clear day from an airplane 2 mi above Earth? Earth's radius is about 4000 mi.

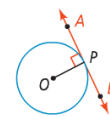
Theorem 12-1

Theorem
If a line is tangent to a circle, then the line is perpendicular to the radius at the point of tangency.

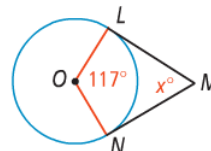
If ...
 \overleftrightarrow{AB} is tangent to $\odot O$ at P



Then ...
 $\overleftrightarrow{AB} \perp \overleftrightarrow{OP}$



Ex. Segment ML and MN are tangent to circle O . What is x ?



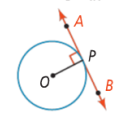
Earth Science The CN Tower in Toronto, Canada, has an observation deck 447 m above ground level. About how far is it from the observation deck to the horizon? Earth's radius is about 6400 km.



Theorem 12-2

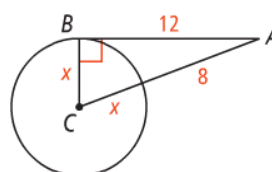
Theorem
If a line in the plane of a circle is perpendicular to a radius at its endpoint on the circle, then the line is tangent to the circle.

If ...
 $\overleftrightarrow{AB} \perp \overleftrightarrow{OP}$ at P

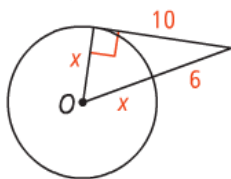


Then ...
 \overleftrightarrow{AB} is tangent to $\odot O$

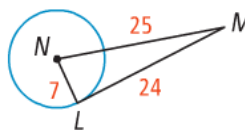
Ex. What is the radius of circle C ?



2 What is the radius of circle O ? Round to the nearest tenth.

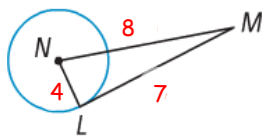


Ex. Is segment ML tangent to circle N at L ? Explain.



3 Is segment ML tangent to circle N at L ?

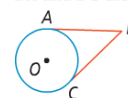
- Yes
- No



Theorem 12-3

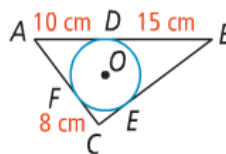
Theorem
If two tangent segments to a circle share a common endpoint outside the circle, then the two segments are congruent.

If ...
 \overline{BA} and \overline{BC} are tangent to $\odot O$



Then ...
 $\overline{BA} \cong \overline{BC}$

Ex. Circle O is inscribed in triangle ABC . What is the perimeter of triangle ABC ?



4 Circle O is inscribed in triangle PQR , which has a perimeter of 88 cm. What is the length of segment QY ?

