

Lesson 6.4 Warm Up

Simplify:

1.  $\sqrt{5x} \cdot \sqrt{8x^2}$

2.  $(2 + \sqrt{3})(4 - 2\sqrt{3})$

3.  $(2xy)^3(4x^2y)$

Lesson 6.4 Rational Exponents (Clickers)

**Essential Understanding:** You can write a radical expression in an equivalent form using a fractional (rational) exponent instead of a radical sign.

In general,  $\sqrt[n]{x} = x^{\frac{1}{n}}$  for any positive integer  $n$ . Like the radical form, the exponent form indicates the principal root.

$$\sqrt{36} = 36^{\frac{1}{2}}$$

$$\sqrt[3]{64} = 64^{\frac{1}{3}}$$

$$\sqrt[4]{16} = 16^{\frac{1}{4}}$$

**Key Concept** Rational Exponent

If the  $n$ th root of  $a$  is a real number,  $m$  is an integer, and  $\frac{m}{n}$  is in lowest terms, then

$$a^{\frac{1}{n}} = \sqrt[n]{a} \text{ and } a^{\frac{m}{n}} = \sqrt[n]{a^m} = (\sqrt[n]{a})^m. \quad \text{If } m \text{ is negative, } a \neq 0.$$

**\*The denominator is the root. The numerator is the exponent.**

**Ex.** What are  $x^{\frac{3}{7}}$  and  $y^{-3.5}$  in radical form?

**Ex.** What are  $\sqrt{a^5}$  and  $(\sqrt[5]{b})^3$  in exponential form?

1 Put the following in radical form.

$$x^{\frac{5}{8}}$$

2 Put the following in radical form.

$$x^{0.2}$$

3 Write the expression in exponential form.

$$\sqrt[4]{x^3}$$

4 Write in exponential form:

$$(\sqrt[5]{y})^4$$



### Properties Properties of Rational Exponents

Let  $m$  and  $n$  represent rational numbers. Assume that no denominator equals 0.

Property	Example	Property	Example
$a^m \cdot a^n = a^{m+n}$	$8^{\frac{1}{3}} \cdot 8^{\frac{2}{3}} = 8^{\frac{1}{3} + \frac{2}{3}} = 8^1 = 8$	$a^{-m} = \frac{1}{a^m}$	$9^{-\frac{1}{2}} = \frac{1}{9^{\frac{1}{2}}} = \frac{1}{3}$
$(a^m)^n = a^{mn}$	$(5^{\frac{1}{2}})^4 = 5^{\frac{1}{2} \cdot 4} = 5^2 = 25$	$\frac{a^m}{a^n} = a^{m-n}$	$\frac{7^{\frac{3}{2}}}{7^{\frac{1}{2}}} = 7^{\frac{3}{2} - \frac{1}{2}} = 7^1 = 7$
$(ab)^m = a^m b^m$	$(4 \cdot 5)^{\frac{1}{2}} = 4^{\frac{1}{2}} \cdot 5^{\frac{1}{2}} = 2 \cdot 5^{\frac{1}{2}}$	$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$	$\left(\frac{5}{27}\right)^{\frac{1}{3}} = \frac{5^{\frac{1}{3}}}{27^{\frac{1}{3}}} = \frac{5^{\frac{1}{3}}}{3}$

Ex. Simplify  $\frac{\sqrt[4]{x^3}}{\sqrt[3]{x^2}}$

Ex. Simplify:

a.  $\frac{\sqrt{x^3}}{\sqrt[3]{x^2}}$

b.  $\sqrt{3}(\sqrt[4]{3})$

5 Simplify:

$\sqrt{7}(\sqrt[3]{7})$

Ex. What is each expression in simplest form?

a.  $(-8x\sqrt{xy})^{\frac{2}{3}}$

b.  $(16y^{-8})^{-\frac{3}{4}}$

6 Write in simplified radical form:

$$(8x^{15})^{\frac{1}{3}}$$

7 Write in simplest radical form:

$$(9^4\sqrt{y})^{\frac{3}{2}}$$