

Lesson 7.4 Warm Up (Clickers)

1. Simplify:  $\sqrt{5} \cdot \sqrt{10}$
2. Write the logarithm for  $5^3 = 125$ .
3. Find  $\log_3 81$ .

Lesson 7.4 Properties of Logarithms

Essential Understanding: Logarithms and exponents have corresponding properties.

**Properties of Logarithms**

For any positive numbers  $m$ ,  $n$ , and  $b$  where  $b \neq 1$ , the following properties apply.

**Product Property**  $\log_b mn = \log_b m + \log_b n$

**Quotient Property**  $\log_b \frac{m}{n} = \log_b m - \log_b n$

**Power Property**  $\log_b m^n = n \log_b m$

What is each expression written as a single logarithm?

1.  $\log_4 32 - \log_4 2$

2.  $6 \log_2 x + 5 \log_2 y$

3.  $\log_4 5x + \log_4 3x$

1 What is the expression as a single logarithm?

$$\log_5 4y - \log_5 2y$$

2 What is the expression written as a single logarithm?

$$2\log_4 6 - \log_4 9$$

Ex. What is each logarithm expanded?

1.  $\log (4x/y)$

2.  $\log_9(x^4/729)$

3.  $\log_3(250/37)$

3 What is the logarithm expanded?

$$\log_3 9x$$

4 What is the logarithm expanded?

$$\log_5(125/x)$$

5 What is the logarithm expanded?

$$\log x^2 y^2$$

You have seen logarithms with many bases. The 'log' key on a calculator find  $\log_{10}$  of a number. To evaluate a logarithm with any base, use the Change of Base Formula.



### Property Change of Base Formula

For any positive numbers  $m$ ,  $b$ , and  $c$ , with  $b \neq 1$  and  $c \neq 1$ ,

$$\log_b m = \frac{\log_c m}{\log_c b}.$$

Ex. What is the value of the expression  $\log_{81} 27$ ?

Solution: Use calculator-- $\log 27 / \log 81$   
 $= 0.75$

Ex. What is the value of  $\log_5 36$ ?

6 What is the value of the expression  $\log_8 32$ ?